

Influence of Anion Charge on Li Ion Diffusion in a New Solid-State Electrolyte, Li_3LaI_6

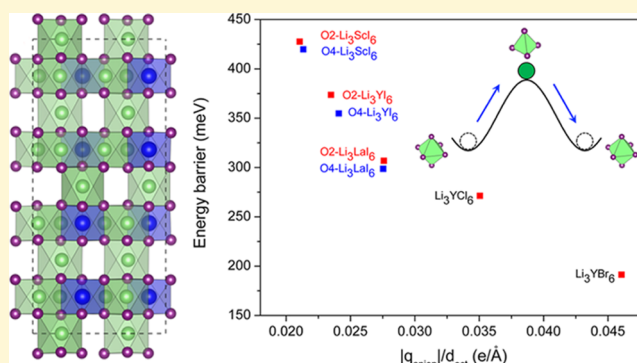
Zhenming Xu,^{||} Xin Chen,[§] Ke Liu,^{||} Ronghan Chen,^{||} Xiaoqin Zeng,^{†,‡,§} and Hong Zhu^{*,†,||} 

[†]State Key Laboratory of Metal Matrix Composites, [‡]School of Materials Science and Engineering, and [§]National Engineering Research Center of Light Alloy Net Forming, Shanghai Jiao Tong University, 800 Dongchuan Road, Shanghai 200240, China

^{||}University of Michigan–Shanghai Jiao Tong University Joint Institute, Shanghai Jiao Tong University, 800 Dongchuan Road, Shanghai 200240, China

Supporting Information

ABSTRACT: Based on density functional theory calculations of iodide-type compounds Li_3MI_6 ($\text{M} = \text{Sc}, \text{Y}, \text{and La}$), Li_3LaI_6 with stable octahedral Li occupation is theoretically found to meet the requirements of high lithium ionic conductivity, deformability, and chemical and electrochemical stability simultaneously, which sulfide-type solid-state electrolytes alone have not achieved so far. The underlying mechanism of superior lithium ion conduction in such a halide superionic conductor with stable octahedral Li occupations compared to the spinel ones with tetrahedral Li occupations has been uncovered. The Li migration enthalpies of those materials with face-centered-cubic anion frameworks are found to be not only strongly related to the ratio of anion charge over bond length ($|q_{\text{anion}}|/d$) but also dependent on the lithium ion coordination number, which could be a universal design principle for searching new superionic conductors.



1. INTRODUCTION

As commercial lithium ion batteries (LIBs) approach their theoretical limits for use in large-scale energy storage applications and also face safety issues, replacing the currently employed liquid electrolytes with solid-state electrolytes (SSEs) and matching with Li metal anode to construct all-solid-state lithium ion batteries (ASSLIBs) not only remarkably enhance the energy density of battery system but increase battery safety as well.^{1–3} Practical ASSLIBs need SSE materials to achieve fast ion conduction with high Li ionic conductivities (10^{-3} – 10^{-2} S/cm) at room temperature. Recent research studies on inorganic superionic conductors have mainly focused on sulfides^{4,5} and oxides.^{6,7} Sulfide-type lithium ionic conductors, compared to the oxide-type ones, show higher ionic conductivities, deformable mechanical flexibilities to realize intimate interface contacts, and the conveniences of synthesizing by cold-pressing. However, sulfide SSE materials are both chemically and electrochemically unstable,^{8,9} which are not only easily oxidized even by dry air but also show frustrating interface compatibilities with LiCoO_2 cathode¹⁰ and Li metal anode.¹¹ On the other hand, oxides are more chemically and electrochemically stable^{8,12} compared to sulfides. Nonetheless, oxides also face some obstacles with respect to their practical applications in ASSLIBs, including relatively low ionic conductivities and inferior deformabilities (poor interface contacts with cathodes).¹³ It is still full of challenges to develop SSE materials with high ionic

conductivities, good deformabilities, and electrochemical stabilities simultaneously.

This motivated us to search for other SSE materials with a better balance between ionic conductivity, deformability, and chemical and electrochemical stability from a refreshed perspective by comprehensively considering the valence state, ionic radius, polarizability, and electronegativity of anions. Compared to the divalent chalcogen anions, the monovalent halogen anions would have weaker Coulomb interactions with Li ions. On the other hand, ionic radii of halogen anions are larger than those of chalcogen anions ($r(\text{Br}^-) = 182$ pm, $r(\text{I}^-) = 206$ pm, $r(\text{O}^{2-}) = 126$ pm, and $r(\text{S}^{2-}) = 170$ pm for six-coordinated anions¹⁴), which lead to longer ionic bond length and higher anionic polarizability¹⁵ and hence simultaneously enhance Li ionic conductivity and deformability. Moreover, halide materials usually show higher electrochemical oxidation and reduction stabilities, and better interfacial compatibilities with high-voltage LiCoO_2 cathode¹⁶ than sulfides, which can be attributed to the higher electronegativity of halogen anions than that of sulfur anion. In the 1980s and 2000s, the spinel-structured halide materials with stable tetrahedral Li occupations were widely studied, such as LiAlCl_4 ,¹⁷ Li_2MgCl_4 ,¹⁸ and Li_2MgBr_4 .¹⁹ However, the advantages of

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halogen anions were not fully demonstrated in these spinel-structured halide materials, whose Li ion conductivities at room temperature are relatively small, on the order of 10^{-3} mS/cm or less. Recently, Asano et al. reported two new lithium halide solid-electrolyte materials, Li_3YCl_6 and Li_3YBr_6 , with stable octahedral Li occupations, exhibiting a high Li ion conductivity of 1 mS/cm at room temperature, as well as high chemical and electrochemical stabilities.¹⁶ Later, Mo et al. used first-principles simulations to investigate Li ion diffusion, electrochemical stability, and interface stability of these two recently reported Li_3YCl_6 and Li_3YBr_6 materials, and theoretically confirmed their high ionic conductivities and good electrochemical stabilities.²⁰ Hence, halide chemistry is a promising new research direction for developing future solid-state electrolytes with fast Li ion transports and good stabilities simultaneously. Meanwhile, a question that arises is that why the new Li_3YCl_6 and Li_3YBr_6 materials with stable octahedral Li occupations can achieve much higher ionic conductivities than the spinel structures with partial tetrahedral Li occupations, although they have similar close packed anion frameworks, e.g., face-centered-cubic (*fcc*) structures.

In this work, we investigated new nonspinel structured lithium ion conducting iodides with stable octahedral Li occupations, Li_3MI_6 ($M = \text{Sc}, \text{Y}, \text{and La}$), based on density functional theory (DFT) calculations. More importantly, the underlying mechanism for the superior Li ion transport in the nonspinel halides to that in the spinel ones was uncovered. Li_3LaI_6 is theoretically predicted to meet the requirements of high Li ionic conductivity, deformability, and chemical and electrochemical stability that sulfide-type SSEs alone have not completely achieved so far, which can be attributed to its long ionic bond length, high anionic polarizability, high stability of LaI_6^{3-} octahedra, and the beneficial Li conduction channel with considerable cation vacancy sites. Therefore, our iodide compound Li_3LaI_6 is quite promising to be utilized as a SSE material for lithium metal–iodine batteries and even ASSLIBs. Moreover, tuning the transition metal elements and strengthen the interactions between Li ion and the crystal lattice framework could effectively enhance Li ion diffusion in Li_3MI_6 with octahedral Li occupations. Such a design principle could be applied for searching new lithium, sodium, or multivalent ion superionic conductors.

2. COMPUTATIONAL METHODS

All calculations were performed using the Vienna *Ab-initio* simulation package (VASP) software, based on the projector-augmented wave method²¹ within the framework of DFT.²² The generalized gradient approximation (GGA)²³ in the form of Perdew–Burke–Ernzerhof exchange functional²² was used. To consider the strong correlation effects of the transition metal in Li_3ScI_6 , Li_3YI_6 , and Li_3LaI_6 halides, both structural optimizations and electronic structure calculations were carried out using the spin-dependent GGA plus Hubbard correction U (GGA + U) method,²⁴ and the effective U_{eff} parameters were 5.00,²⁵ 3.00,²⁶ and 10.32 eV²⁷ for the Sc 3d, Y 4d, and La 4f states, respectively. The plane-wave energy cutoff was set to 520 eV. The Monkhorst–Pack method²⁸ with $3 \times 2 \times 1$ and $6 \times 4 \times 2$ k -point meshes was employed for the Brillouin zone sampling of Li_3MI_6 ($M = \text{Sc}, \text{Y}, \text{and La}$) unit cells, respectively, for structural relaxations and electronic structure calculations. The convergence criteria of energy and force were set to 10^{-5} eV/atom and 0.01 eV/Å, respectively.

The chemical and electrochemical stability of a material can be theoretically evaluated by the compositional phase diagram and lithium grand potential phase diagram,²⁹ respectively, constructed by the Pymatgen code based on the DFT ground-state energies of the

corresponding compounds from the Materials Project open database.^{30,31} Phonon calculations were carried out using the Cambridge Sequential Total Energy Package (CASTEP)³² software based on the density functional perturbation theory.³³ The sets of the exchange functional, plane-wave energy cutoff, and k -mesh for CASTEP were the same as those for VASP. Activation energy barriers and diffusion coefficients of Li were calculated by the climbing image nudged elastic band (CI-NEB) method³⁴ and elevated-temperature *Ab-initio* molecular dynamics (AIMD) simulations.³⁵ A smaller plane-wave energy cutoff of 300 eV was chosen for AIMD simulations of the $2 \times 1 \times 1$ Li_3MI_6 ($M = \text{Sc}, \text{Y}, \text{and La}$) supercells with a Gamma-centered $1 \times 1 \times 1$ k -point grid. The time step was set to 2 fs, and all supercell systems were simulated for 20000 steps with a total time of 40 ps in a statistical ensemble with a fixed particle number, volume, and temperature (NVT). The charge analyses were performed by the Hirshfeld method³⁶ as implemented in CASTEP software.

3. RESULTS AND DISCUSSION

3.1. Crystal Structure and Stability. Our predicted monoclinic Li_3MI_6 ($M = \text{Sc}, \text{Y}, \text{and La}$) (in the $C2$ space group) have layered structures with O4 stacking patterns along the c -direction, denoted as O4- Li_3MI_6 , where O represents MI_6 octahedra, and 4 represents the stacking sequences of ABCD for I anion layers, as shown in Figure 1. DFT-optimized lattice

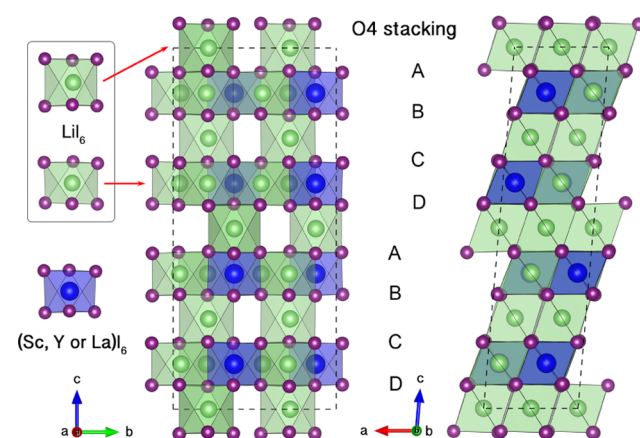


Figure 1. Unit cells of Li_3MI_6 ($M = \text{Sc}, \text{Y}, \text{and La}$) crystal with the O4 stacking sequences (LiI_6 octahedra in the transition metal layer and in the pure Li layer have different volumes). These crystal structure plots are displayed by the VESTA software.³⁷

constants and atomic positions of the unit cells of Li_3MI_6 ($M = \text{Sc}, \text{Y}, \text{and La}$) are listed in Tables S1 and S2 in Supporting Information. The other two possible stacking sequences of Li_3MI_6 ($M = \text{Sc}, \text{Y}, \text{and La}$) were considered, including the O1 stacking of AA pattern (space group: $P2_1/m$) and the O2 stacking of ABAB pattern (space group: $C2/c$) (see Figure S1). DFT energies of O1- Li_3MI_6 ($M = \text{Sc}, \text{Y}, \text{and La}$) are slightly higher than those of O4 phases by 8.45, 8.61, and 8.27 meV/atom, respectively, and the corresponding energies of O2- Li_3MI_6 ($M = \text{Sc}, \text{Y}, \text{and La}$) are also slightly higher than those of O4 phases by 2.41, 2.60, and 2.44 meV/atom, respectively. Such small energy differences, much lower than the room-temperature $k_B T$ of ~ 26 meV/atom, indicate that O1, O2, and O4 structures are much likely to coexist in the experimentally synthesized Li_3MI_6 materials. To better understand the effects of the stacking sequences on Li ion diffusion, the slightly unstable O2- Li_3MI_6 ($M = \text{Sc}, \text{Y}, \text{and La}$) phases were also studied together with O4 phases.

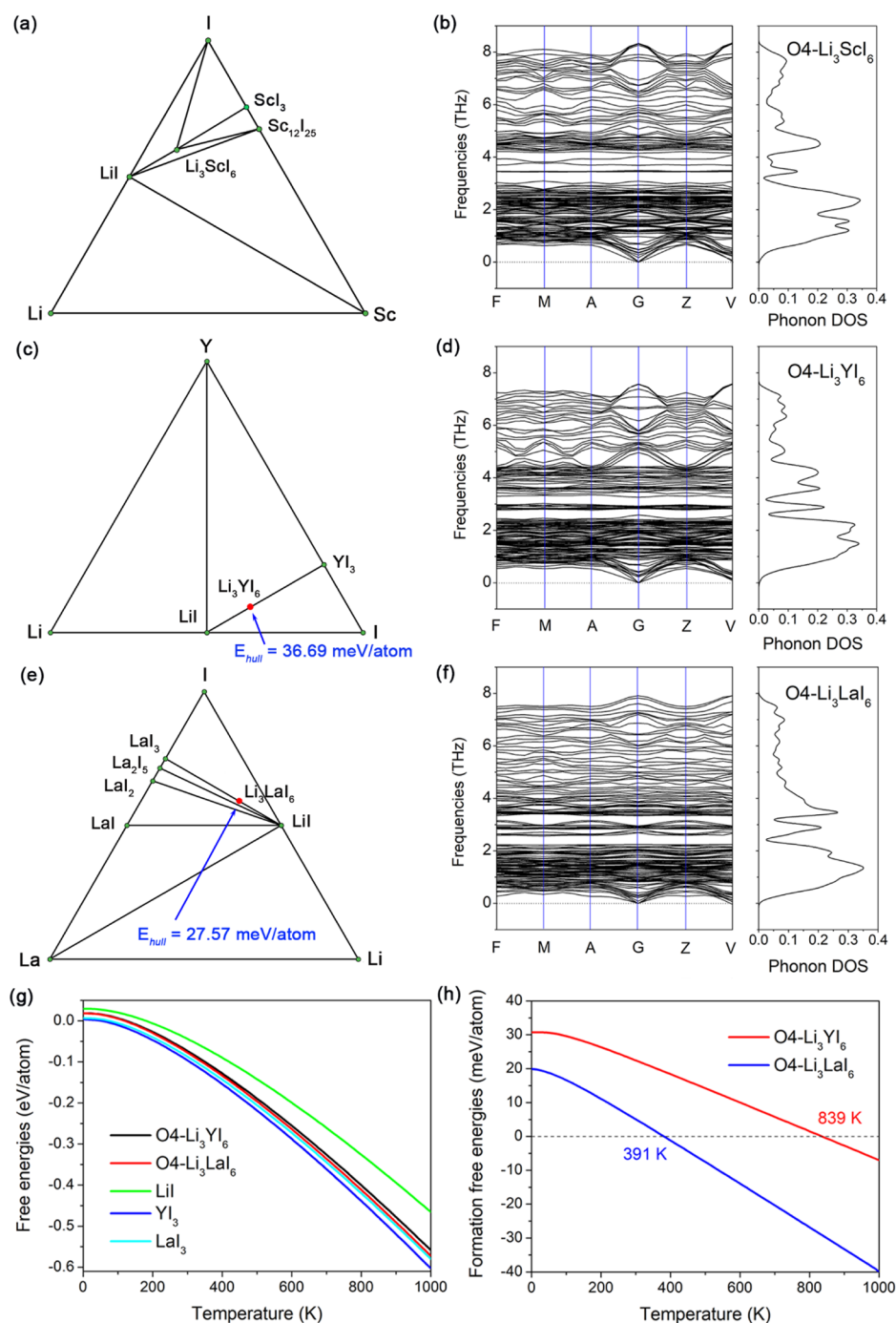


Figure 2. Thermodynamic and dynamic stabilities of O4-Li₃MI₆ (M = Sc, Y and La) materials. (a) DFT-calculated Li–Sc–I phase diagram; the green dots represent the stable compounds (O4-Li₃ScI₆ is stable in its ternary system), (c) DFT-calculated Li–Y–I phase diagram; O4-Li₃YI₆ phase is slightly higher in energy (energy above hull is 36.69 meV per atom) with respect to that of the ground-state mixtures of LiI and YI₃, (e) DFT-calculated Li–La–I phase diagram; O4-Li₃LaI₆ phase is slightly higher in energy (energy above hull is 27.57 meV per atom) with respect to that of the ground-state mixtures of LiI and LaI₃; (b), (d), and (f) phonon dispersions and total phonon density of states (DOS) of O4-Li₃ScI₆, O4-Li₃YI₆, and O4-Li₃LaI₆, respectively; (g) calculated temperature-dependent formation energies (Helmholtz free energies) of O4-Li₃YI₆ and O4-Li₃LaI₆ materials, and (h) Helmholtz free energies of O4-Li₃YI₆ and O4-Li₃LaI₆ as well as their equilibrium phases, LiI, YI₃, and LaI₃. O4-Li₃YI₆ and O4-Li₃LaI₆ are thermodynamically stable and can be entropically stabilized above 839 and 391 K, respectively.

Figures 1 and S1 show that there are 1/3 octahedral vacancy sites in the stoichiometric Li₃MI₆, benefitting Li ion diffusion. There are two kinds of stable Li occupation sites, namely, octahedral sites in the transition metal layer and in the pure lithium layer, respectively. These two kinds of LiI₆ octahedra have different volumes (different Li–I bond lengths), and the volumes of LiI₆ octahedra in the transition metal layer are

slightly larger than those in the pure lithium layer. For the convenience of experimental structural characterization, the simulated X-ray diffraction pattern and calculated Raman spectra with characteristic vibration modes of O4- and O2-Li₃MI₆ (M = Sc, Y, and La) are provided in Figures S2 and S3.

The thermodynamic stabilities of Li₃MI₆ were specifically studied by constructing the Li–M–I ternary compositional

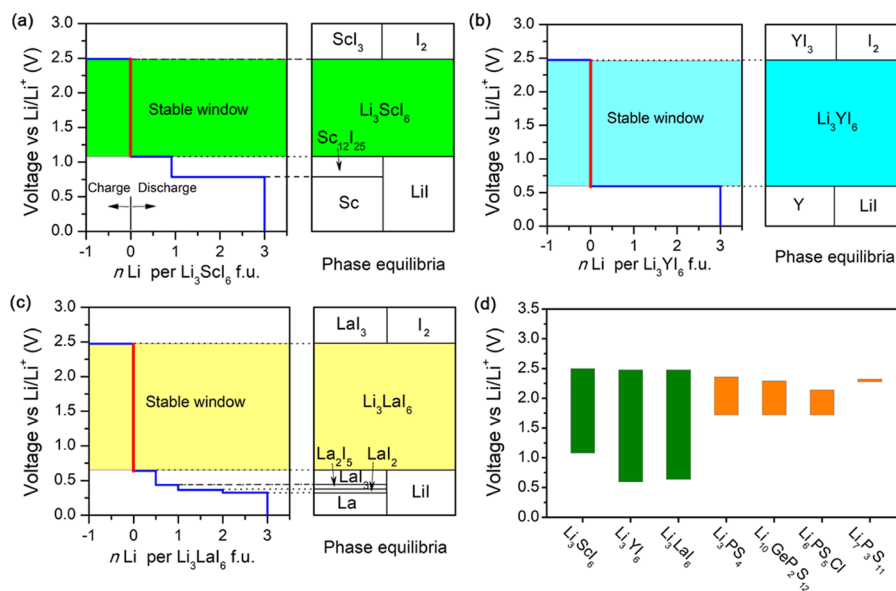


Figure 3. DFT-calculated voltage profiles (with respect to the chemical potential of Li metal) and phase equilibria of (a) O4-Li₃ScI₆, (b) O4-Li₃YI₆ and (c) O4-Li₃LaI₆ upon lithiation (Li metal insertion, $n > 0$) and delithiation (Li metal extraction, $n < 0$) based on the analyses of lithium grand potential phase diagrams, (d) DFT-calculated electrochemical windows of O4-Li₃MI₆ (M = Sc, Y, and La) iodides and other sulfide-type superionic conductors.

phase diagrams based on DFT-calculated energies³⁸. Because O4- and O2-Li₃MI₆ phases have almost same DFT energies, here we only made thermodynamic stability analyses for O4-Li₃MI₆. A green dot in the DFT compositional phase diagrams (Figure 2) represents a stable compound whose energy is lower than that of any other compound at that composition. The Li–Sc–I phase diagram in Figure 2a shows that O4-Li₃ScI₆ phase is thermodynamically stable at 0 K with respect to its phase equilibrium compounds, LiI and ScI₃. We expect that the actual formation energy of Li₃ScI₆ at elevated temperatures could be even lower due to the entropic contributions. In addition, no imaginary vibrational mode is observed from the phonon dispersions of O4-Li₃ScI₆ (Figure 2b) and O2-Li₃ScI₆ (Figure S4a), indicating that both O4- and O2-Li₃ScI₆ are dynamically stable. Therefore, Li₃ScI₆ can be feasibly synthesized by the spontaneous reaction of its phase equilibrium compounds.

However, Figure 2c,e show that DFT energies of O4-Li₃YI₆ and O4-Li₃LaI₆ are slightly higher than those of the corresponding two-phase mixtures of LiI and YI₃ (LaI₃) by 36.69 and 27.57 meV/atom, respectively, which may be stabilized by the entropic contributions at elevated temperatures, such as lattice vibrational entropies. No imaginary vibrational mode is observed from the phonon dispersions of O4-Li₃YI₆, O4-Li₃LaI₆, O2-Li₃YI₆, and O2-Li₃LaI₆ (Figures 2d,f and S4b,c), which means that both Li₃YI₆ and Li₃LaI₆ are dynamically stable. By computing the lattice vibrational entropies of O4-Li₃YI₆, O4-Li₃LaI₆, YI₃, LaI₃, and LiI, the Helmholtz free energies as a function of temperature of these five compounds were obtained (Figure 2g). The formation free energies (E_f) of O4-Li₃MI₆ were calculated by $E_f(\text{O4-Li}_3\text{MI}_6) = F(\text{O4-Li}_3\text{MI}_6) - 3F(\text{LiI}) - F(\text{MI}_3)$. The temperature-dependent E_f of O4-Li₃YI₆ and O4-Li₃LaI₆ are shown in Figure 2h, indicating that O4-Li₃YI₆ and O4-Li₃LaI₆ are entropically stabilized above 839 and 391 K, respectively. Similarly, O2-Li₃YI₆ or O2-Li₃LaI₆ might be more stable at higher temperatures than the O4 phases. Our formation energy calculations suggest that Li₃YI₆ and Li₃LaI₆ are stable at

elevated temperatures. Moreover, the elastic constants of Li₃MI₆ (M = Sc, Y, and La) were calculated to verify their mechanical properties,³⁹ as summarized in Table S3. All of these elastic constants comply well with the Born criteria for a mechanically stable monoclinic crystal,^{40,41} confirming the mechanical stabilities of Li₃MI₆. In addition, the elastic properties of electrolyte material are crucial parameters for designing SSLIBs.⁴² A model proposed by Monroe et al. demonstrated that SSE materials with shear moduli twice that of lithium metal can effectively suppress the growth of lithium dendrites.⁴³ From the comparisons in Table S3, all calculated B , E , and G moduli of Li₃MI₆ are larger than twice that of Li metal,⁴⁰ suggesting that Li₃MI₆ would mechanically block the growth of lithium dendrites. Based on the above analyses of thermodynamic, dynamic, and mechanical stabilities, we can conclude that these three Li₃MI₆ (M = Sc, Y, and La) materials are much likely to be experimentally synthesized.

3.2. Electrochemical Stability. The calculated band gaps of Li₃MI₆ (M = Sc, Y, and La) are in the range 2.86–3.58 eV, which can effectively insulate electron transport.⁴⁴ The element-projected band structures and density of states (Figure S5) show that the valence band maxima of Li₃MI₆ are dominated by I[−] anion, which will be the first specie to be oxidized at high voltages. The conduction band minima of Li₃MI₆ are dominated by M³⁺ cation, which can be further reduced to M metal at low voltages. It is important to note that the band gap analyses only provide an upper limit of electrochemical stability.

During cycling operations of solid-state lithium batteries, the quite high lithium chemical potential at the anode side induces the reduction reactions of SSE materials with Li insertion, and the low lithium chemical potential (a strong oxidizing environment) at the charged cathode side would strongly oxidize SSEs with Li extraction.²⁹ Lithium grand potential phase diagrams, containing phase equilibrium with respect to the applied lithium potential,³⁸ were constructed to assess the electrochemical stabilities of O4-Li₃MI₆ (M = Sc, Y, and La). Because the construction of lithium grand potential phase

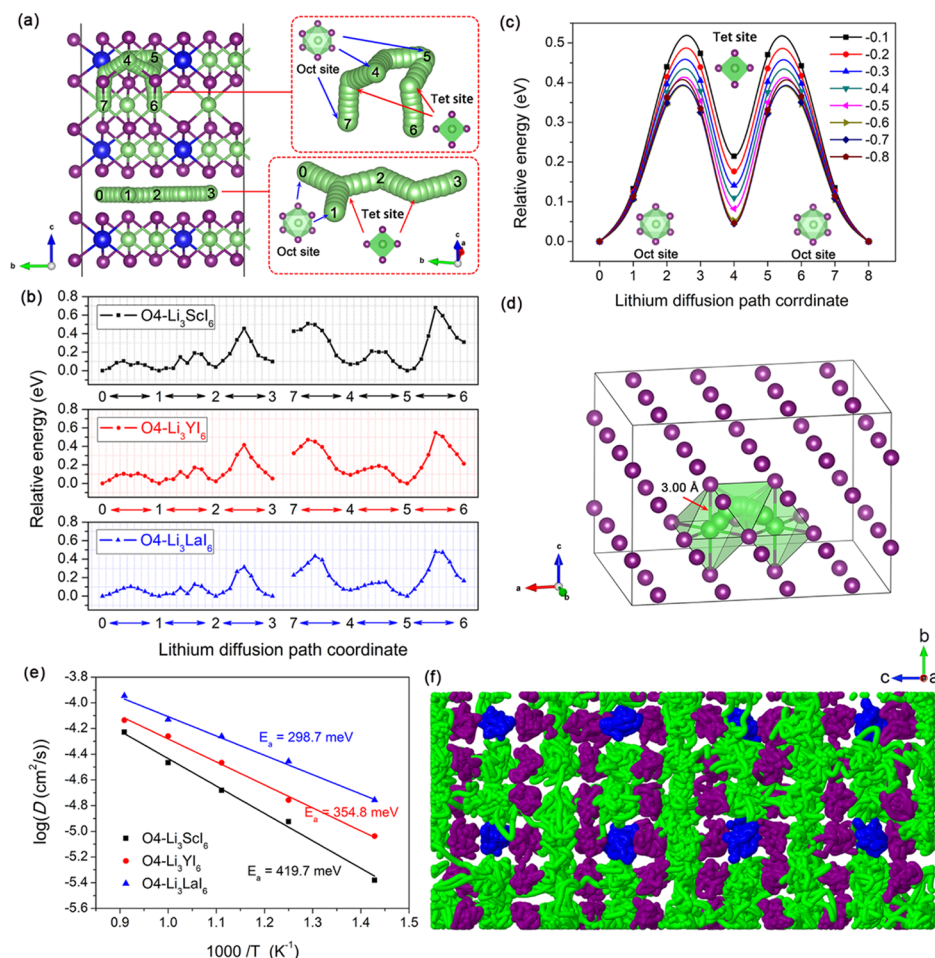


Figure 4. CI-NEB calculations and AIMD simulations for O4-Li₃MI₆ (M = Sc, Y, and La). (a) Seven different Li ion diffusion paths, including the intralayer paths (0 ↔ 1, 1 ↔ 2, 2 ↔ 3, and 4 ↔ 5) and crosslayer paths (4 ↔ 7 and 5 ↔ 6); the crystal structure plots are displayed using the VESTA software;³⁷ (b) energy variations of Li ion diffusion in O4-Li₃MI₆; (c) CI-NEB-calculated energy variations and (d) structural model of Li ion diffusion from one octahedral site to its adjacent octahedral site through a transition state with respect to different I anion charges in an *fcc* I sublattice with a single Li⁺ ion (Li–I bond length in the octahedron is set to a constant of 3.00 Å). Only the migrating Li ion is allowed to relax whereas other anions are fixed; (e) Arrhenius plot of Li ion diffusion coefficient at different temperatures for O4-Li₃MI₆ (M = Sc, Y, and La); and (f) atomic trajectories from 900 K AIMD simulations of O4-Li₃LaI₆, displayed using the Jmol code,⁴⁶ where green, blue, and purple balls represent Li, La, and I atoms, respectively.

diagram is based on DFT energies, and O4- and O2-Li₃MI₆ phases have almost same DFT energies, we only focus on the relatively stable O4-Li₃MI₆ phases to represent Li₃MI₆ materials in the lithium grand potential phase diagram analyses. Based on the constructed lithium grand potential phase diagrams of the Li–M–I ternary systems, we obtained DFT-calculated voltage profiles and phase equilibria of O4-Li₃MI₆ (M = Sc, Y, and La) upon lithiation and delithiation, as depicted in Figure 3. From Figure 3a, when the voltage is higher than 2.49 V, the active I[−] anion in Li₃ScI₆ will be oxidized to I₂ and the ScI₃ phase with Li extraction. However, Li₃ScI₆ begins to be lithiated at 1.08 V, and decomposes into LiI and the Sc₁₂I₂₅ phase. When the voltage is further decreased to 0.784 V, the formed Sc₁₂I₂₅ begins to be further reduced to Sc metal and LiI upon lithiation. Therefore, the calculated electrochemical window of Li₃ScI₆ is from 1.08 to 2.49 V, with a window width of 1.41 V. Similar redox reactions can also be found for O4-Li₃YI₆ and Li₃LaI₆ (Figure 3b,c). The electrochemical windows of Li₃YI₆ and Li₃LaI₆ are 1.93 and 1.83 V, ranging from 0.55 to 2.48 V and from 0.64 to 2.47 V, respectively. Figure 3d shows that the electrochemical window

widths of Li₃MI₆ (M = Sc, Y, and La) iodides are much larger than those (0.10–0.75 V) of sulfides, indicating that Li₃MI₆ iodides have much higher electrochemical stabilities and better compatibilities with electrodes than sulfides, especially their antireduction stabilities. The above electrochemical stability analyses are from the perspective of the thermodynamic driving force for decomposition reaction. However, the kinetic factors, including the morphology, electronic and ionic conductivity of the decomposition products, and the applied current, are very important in determining the extent of decomposition reaction,⁸ which were not considered here. We believe the formed electronically insulating but ionically conducting interphases of Li₃MI₆ (M = Sc, Y, and La) (see details in the Supporting Information) can effectively extend their electrochemical stability windows by the limited kinetics of decomposition reaction.

3.3. Lithium Ion Diffusivity and Conductivity. A high ionic conductivity of 10^{−3}–10^{−2} S/cm at room temperature is the first requirement for the application of ionic conductors as SSEs for ASSLIBs. In this section, Li ion diffusivities and conductivities of Li₃MI₆ were investigated by the CI-NEB

calculations and AIMD simulations.⁴⁵ Li ion diffusion in Li_3MI_6 is mainly based on the vacancy diffusion mechanism, due to the abundant octahedral vacancy sites in the stoichiometric Li_3MI_6 unit cells (Figures 1 and S1). Because O4- Li_3MI_6 iodides have different Li occupation environments, we considered five different paths for Li ion diffusion from one octahedron site to its adjacent octahedron site through a transition state, as shown in Figure 4a, including the intralayer paths ($0 \leftrightarrow 1$, $1 \leftrightarrow 2$, $2 \leftrightarrow 3$, and $4 \leftrightarrow 5$) and crosslayer paths ($4 \leftrightarrow 7$ and $5 \leftrightarrow 6$). The calculated energy variations of Li ion diffusion in O4- Li_3MI_6 ($M = \text{Sc}$, Y , and La) by the CI-NEB method are shown in Figure 4b, and the corresponding energy barriers for different diffusion paths are listed in Table S5. The activation energy barriers of the crosslayer paths are relatively higher than those of the intralayer paths, indicating that Li ion diffusion within the x - y plane is slightly easier than that along the z -direction. Overall, the activation energy barriers of Li ion diffusion along each path in O4- Li_3MI_6 ($M = \text{Sc}$, Y , and La) follow the order of $\text{Li}_3\text{ScI}_6 > \text{Li}_3\text{YI}_6 > \text{Li}_3\text{LaI}_6$, indicating that the heavier the transition metal M (with the same valence state), the easier the Li ion diffusion in O4- Li_3MI_6 .

Recent works on superionic conductors have demonstrated the influence of lattice dynamic that softer lattices would lead to lower activation barriers for ion diffusion. In other words, fast lithium ion conductors usually show low lithium vibration frequencies or low center of lithium phonon density of states (DOS).⁴⁷ Here, we have also calculated the partial phonon density of states of Li atom in O4- and O2- Li_3MI_6 ($M = \text{Sc}$, Y , and La) and obtained their corresponding phonon DOS centers, as shown in Figure S7. For both O4- and O2- Li_3MI_6 , the phonon DOS centers follow the trend of $\text{Li}_3\text{LaI}_6 < \text{Li}_3\text{YI}_6 < \text{Li}_3\text{ScI}_6$, which is fully consistent with the order of bulk moduli in Table S3 and the activation energy barriers from CI-NEB calculations. In addition, the phonon band centers of O4- Li_3MI_6 ($M = \text{Sc}$, Y , and La) are slightly lower than those of O2-types, in accordance with the bulk moduli of O4-types being smaller than those of O2-types in Table S3.

Considering that the activation energy barriers from the CI-NEB calculations are diffusion-path-dependent, CI-NEB calculations cannot provide the total activation energy barrier as experiments. Therefore, we performed AIMD simulations to further understand Li ion diffusion in Li_3MI_6 and obtain the total activation energy barriers. Figures 4e and S8 show the Arrhenius plots of Li ion diffusion coefficients at different elevated temperatures of O4- and O2- Li_3MI_6 ($M = \text{Sc}$, Y , and La), respectively. The overall activation energy barriers of Li ion diffusion in O4- Li_3MI_6 ($M = \text{Sc}$, Y , and La) are calculated to be 419.7, 354.8, and 298.7 meV, respectively (Table S6). In addition, the overall Li diffusion activation energy barriers of O2- Li_3MI_6 ($M = \text{Sc}$, Y , and La) are 426.3, 372.2, and 305.5 meV, respectively. The extrapolated Li ion diffusion coefficients at 300 K of O4- Li_3MI_6 ($M = \text{Sc}$, Y , and La) are 3.84×10^{-10} , 3.51×10^{-9} , and $2.40 \times 10^{-8} \text{ cm}^2/\text{s}$, respectively, and the corresponding ionic conductivities are 0.02, 0.19, and 1.23 mS/cm, respectively (Table S6). And Li ion diffusion coefficients at 300 K of O2- Li_3MI_6 ($M = \text{Sc}$, Y , and La) are 4.40×10^{-10} , 2.43×10^{-9} , and $1.94 \times 10^{-8} \text{ cm}^2/\text{s}$, respectively, and the corresponding ionic conductivities are 0.03, 0.13, and 0.99 mS/cm, respectively. It can be seen that O4- Li_3MI_6 have slightly higher extrapolated ionic conductivities than O2-types at room temperature. The room-temperature ionic conductivities of 0.99–1.23 mS/cm of Li_3LaI_6 are comparable to those of the state-of-the-art sulfide-type solid electrolytes, such as

LGPS and LPS. The atomic trajectories in Figure 4f show that the steady I anion frameworks are well maintained, and no breaking of M–I bonds is observed during the entire 900 K AIMD simulations. Moreover, the mean-square-displacement (MSD) data (Figure S9) and atomic trajectories of Li (Figure S10) clearly exhibit significant three-dimensional (3D) Li hopping. The CI-NEB calculations and AIMD simulations demonstrate that Li_3LaI_6 is a 3D superionic conductor, which meets the first requirement of high ionic conductivity of 10^{-3} – 10^{-2} S/cm at room temperature and is highly promising to be utilized as a SSE material.

3.4. Influence of Anionic Charge on Lithium Ion Diffusion. Usually, the measured activation energy barrier (E_a) is the sum ($E_a = \Delta H_m + 0.5H_f$) of the migration enthalpy change (ΔH_m) and the defect formation enthalpy (H_f).^{48,49} In a lithium superionic conductor, the Li defect formation enthalpy is often negligibly small, and the measured E_a can be approximated by ΔH_m value.⁴⁹ Furthermore, according to our previous research studies on the chalcopyrite-structured LiMS_2 (M represents 3d transition metals from Sc to Ni),⁵⁰ the charge and bond length dependent Coulombic interactions between Li cation and its adjacent S anions significantly affect Li ion diffusion. To better understand the lithium diffusion mechanism in the nonspinel Li_3MI_6 , where I atoms form an *fcc* sublattice and Li atoms occupy the octahedral central sites, we studied the correlation of E_a vs the potential difference (E_p) between the tetrahedral central site (transition state, E_{tet}) surrounded by four I anions and its adjacent octahedral central site (equilibrium state, E_{oct}) surrounded by six I anions in an *fcc* I anion sublattice model, which allows us to directly assess the effects of anion.⁵¹ Since the octahedral centers are the stable Li occupation sites in our nonspinel Li_3MI_6 ($E_{\text{tet}} > E_{\text{oct}}$ or $E_p > 0$), a smaller E_p leads to a smaller H_m (Figure S11). The total potential of a reference positive ion, interacting with all other anions in an *fcc* I anion sublattice, approximately equals the sum of the non-electrostatic potential and the total electrostatic potential of all Li–I pairs. Therefore, we obtained

$$E_a \approx \Delta H_m \propto E_p = E_{\text{tet}} - E_{\text{oct}} \approx [C_1 - \sum_{i=1}^n \frac{e^2 |q_i|}{4\pi\epsilon d_i}] - [C_2 - \sum_{j=1}^n \frac{e^2 |q_j|}{4\pi\epsilon d_j}] \approx C - \frac{e^2}{4\pi\epsilon} \left[\sum_{i=1}^n \frac{1}{d_i} - \sum_{j=1}^n \frac{1}{d_j} \right] \times |q_1| \approx C - \frac{Ae^2}{4\pi\epsilon} \left(\frac{|q_1|}{d_{\text{oct}}} \right)$$

, where the reference ion of Li is assumed to have one charge e , C_1 and C_2 are the non-electrostatic potentials, ϵ is the dielectric constant, q_i is the charge of an I anion, d_i are the distances between the tetrahedral Li site and its i th-neighbor I anions, d_j are the distances between the octahedral Li site and its j th-neighbor I anions, C is a positive constant ($C = C_1 - C_2$); $\left[\sum_{i=1}^n \frac{1}{d_i} - \sum_{j=1}^n \frac{1}{d_j} \right]$ is convergent to a positive constant A/d_{oct} as shown in Figure S12, and d_{oct} is the distance between the octahedral Li site and its first nearest-neighbor I anion. It can be seen that the larger values of $|q_1|/d_{\text{oct}}$ result in smaller E_p , consequently reducing E_a for the octahedral Li ion diffusion.

In contrast, for Li ion diffusion in the spinel halides usually from one tetrahedral equilibrium site to another tetrahedral equilibrium site through an octahedral transition state, we can

obtain $E_a \propto E_{\text{oct}} - E_{\text{tet}} \approx C' + \frac{Ae^2}{4\pi\epsilon} \left(\frac{|q_{\text{anion}}|}{d_{\text{tet}}} \right)$, where C' is a positive constant, q_{anion} is the charge of the anion, and d_{tet} is the distance between the tetrahedral central site and its first nearest-neighbor anion. It can be clearly found that the larger values of $|q_{\text{anion}}|/d_{\text{tet}}$ give rise to an increase in E_p , leading to higher E_a for the tetrahedral Li ion diffusion. For the spinel-structured LiAlCl_4 , Li_2MgCl_4 , and Li_2MgBr_4 , the very active Mg and Al elements with smaller ionic radii correspond to larger $|q_{\text{Cl}}|/d_{\text{tet}}$ and $|q_{\text{Br}}|/d_{\text{tet}}$ ratios, eventually resulting in higher E_a and poor ionic conductivities. This similar effect can also be found in $\text{Li}_{10}\text{MP}_2\text{S}_{12}$ ($M = \text{Ge}$ and Sn) with stable tetrahedral Li occupations. The lower electronegativity of Sn vs Ge (10.2 vs 11.1)⁵² gives rise to more electrons on S anions in $\text{Li}_{10}\text{SnP}_2\text{S}_{12}$,⁵³ leading to the larger $|q_{\text{S}}|/d$ value, as shown in Table S7, and thereby increases its E_a compared to those of $\text{Li}_{10}\text{GeP}_2\text{S}_{12}$, which are in good accordance with AIMD simulations by Ong et al.⁵⁴

The atomic Hirshfeld charges and Li–I bond lengths of Li_3MI_6 were calculated, as shown in Table S8 and Figure S13, respectively. Atomic Hirshfeld charges indicate that the charges of I anion for both O4- and O2-structures slightly increase from Li_3ScI_6 to Li_3LaI_6 . This is because La atom is the most active one among the elements of group IIIB (Sc ($\chi_A = 7.0$) > Y ($\chi_A = 6.3$) > La ($\chi_A = 6.0$)⁵²), which can donate more electrons to its adjacent I anions. The Gaussian distributions of Li–I bond lengths show that the average bond lengths are 3.00, 3.03, and 3.06 Å for O4- Li_3MI_6 ($M = \text{Sc}$, Y , and La), respectively, and 3.05, 3.06, and 3.08 Å for O2- Li_3MI_6 ($M = \text{Sc}$, Y , and La), respectively. Although the Li–I bond lengths of Li_3LaI_6 are slightly larger than those of Li_3MI_6 ($M = \text{Sc}$ and Y), the $|q_{\text{I}}|/d_{\text{oct}}$ value of Li_3LaI_6 is still the largest, and the $|q_{\text{I}}|/d_{\text{oct}}$ values follow the order of $\text{Li}_3\text{LaI}_6 > \text{Li}_3\text{YI}_6 > \text{Li}_3\text{ScI}_6$ (Figure 5),

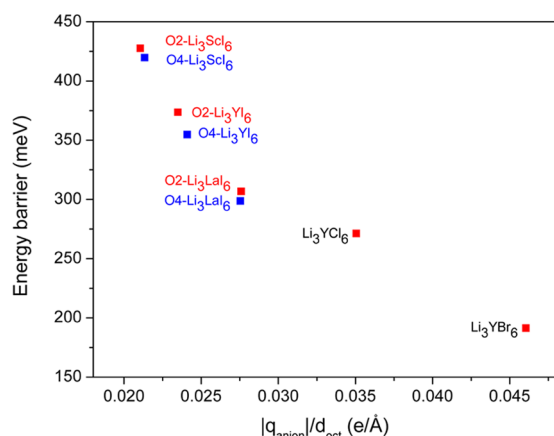


Figure 5. $|q_{\text{anion}}|/d_{\text{oct}}$ -dependent activation energy barriers for Li ion diffusion in O4- Li_3MI_6 , O2- Li_3MI_6 ($M = \text{Sc}$, Y , and La), Li_3YCl_6 , and Li_3YBr_6 , respectively, where Li takes octahedral sites.

which is consistent with the sequences of anion charge. Hence, the anion charges play more crucial roles in determining the $|q_{\text{I}}|/d_{\text{oct}}$ values than the Li–I bond length (bottleneck areas, Table S6) in Li_3MI_6 materials. This larger $|q_{\text{I}}|/d_{\text{oct}}$ value of Li_3LaI_6 would result in the lower phonon DOS center of Li, corresponding to the smaller E_p between LiI_4 tetrahedra and LiI_6 octahedra and hence the lower E_a for Li ion diffusion. The recently reported Li_3YCl_6 and Li_3YBr_6 superionic conductors with stable octahedral Li occupations also show relatively larger $|q_{\text{Cl}}|/d_{\text{oct}}$ and $|q_{\text{Br}}|/d_{\text{oct}}$ ratios (Figure 5), and this may be

why ion transport in these new nonspinel structures is superior to that in the spinel-structured halides with tetrahedral Li occupations, although they have the same *fcc* anion frameworks. In addition, the $|q_{\text{Cl}}|/d_{\text{oct}}$ value of Li_3YCl_6 is larger than the $|q_{\text{Br}}|/d_{\text{oct}}$ value of Li_3YBr_6 , making the activation barrier of Li_3YCl_6 lower than that of Li_3YBr_6 , which is consistent with the results from 500 K AIMD simulations by Mo et al.²⁰

To further verify the anion charge dependent E_p , we have monitored the energy variations (Figure 4c) of Li ion diffusion from one octahedral site to its adjacent octahedral site through a transition state with respect to different I anion charges in a *fcc* I sublattice, in which only one migrating Li^+ ion was considered (Figure 4d). This similar calculation method can also be found in the previous work by Ceder et al.⁵¹ Figure 4c shows that E_p between LiI_4 tetrahedron and LiI_6 octahedron decreases with the increase of I anion charge, resulting in a lower E_a for the system with more negatively charged anions. Therefore, we can conclude that the electronegativity of M element has a fundamental impact on Li ion diffusion in Li_3MI_6 , and the smaller electronegativity of La atoms makes faster Li ion diffusion in Li_3LaI_6 .

Here, based on the profound understandings of Li_3MI_6 and other reported superionic conductors, we identified an alternative design principle for searching new ternary lithium superionic conductors with octahedral occupations, which can also be applied to sodium or multivalent ion superionic conductors. The large electronegativity difference between the anion element and non-lithium cation element leading to large $|q_{\text{anion}}|/d_{\text{oct}}$ values is essential for achieving extremely fast lithium ion diffusion in a superionic conductor with Li octahedral occupations, as depicted in Figure 5, and the corresponding non-lithium cation element M should locate at the left bottom of the periodic table with a small electronegativity and a large atomic number.

4. CONCLUSIONS

In this work, Li_3LaI_6 with stable octahedral Li occupations is theoretically found to simultaneously meet the requirements of high lithium ionic conductivity, deformability, and chemical and electrochemical stability that sulfide-type SSEs alone have not completely achieved so far. Our DFT calculations demonstrate that Li_3LaI_6 superionic conductor is promising to be experimentally synthesized and utilized as a solid-state electrolyte material for all-solid-state lithium ion batteries with a wider electrochemical window than that of sulfides and high ionic conductivities of 1.23–2.08 mS/cm, comparable to those of the state-of-the-art sulfide-type solid electrolytes, such as $\text{Li}_{10}\text{GeP}_2\text{S}_{12}$ and Li_3PS_4 . The underlying mechanism of superior Li ion conduction in such halide superionic conductors with stable octahedral Li occupations compared to the spinel ones with tetrahedral Li occupations has been uncovered. A relationship between the migration enthalpy and anion charge for those materials with face-centered-cubic anion frameworks has been identified: (1) a large $|q_{\text{anion}}|/d_{\text{oct}}$ ratio favors Li ion hopping between the equilibrium octahedral sites through tetrahedral transition site; (2) a small $|q_{\text{anion}}|/d_{\text{tet}}$ ratio is beneficial to the Li diffusion between tetrahedral sites through octahedral transition sites. Such a design principle could be applied for searching new lithium, sodium, or multivalent ion superionic conductors. For example, in a ternary lithium ion conductor with stable Li octahedral occupations, a larger electronegativity difference between the anion element and

non-lithium cation element is essential to obtain large $|q_{\text{anion}}|/d_{\text{oct}}$ ratios and hence to enhance lithium-ion conductivity.

■ ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.chemmater.9b02075.

Structural information; phonon dispersions and DOS; elastic constants and elastic properties; electronic structures; electrochemical stability against electrodes; Li ion diffusion properties; total and direction projected MSD; atomic trajectories of AIMD simulations; atomic Hirshfeld charges (PDF)

■ AUTHOR INFORMATION

Corresponding Author

*E-mail: hong.zhu@sjtu.edu.cn.

ORCID

Hong Zhu: 0000-0001-7919-5661

Notes

The authors declare no competing financial interest.

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